



# UNDERSTANDING SOFTWARE DEV USING EQUATIONS

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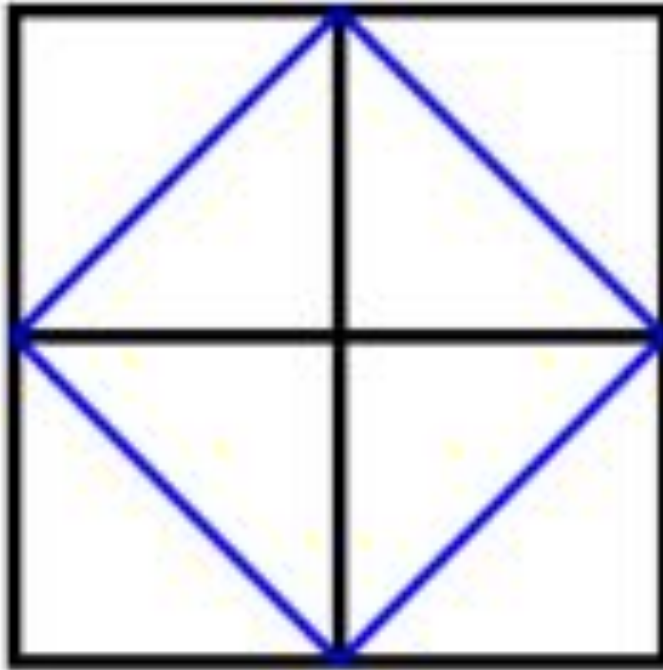
# Software engineering is:

- Hard!
- Non-intuitive
- Misunderstood
- Seen as black-art done by amateurs

# Typical problems

- Congestion and Dependencies
- Technical Debt
- Firefighting

**How can math help us?**



Socrates' Meno

**Clear thinking**  
*rather than precise proofs*

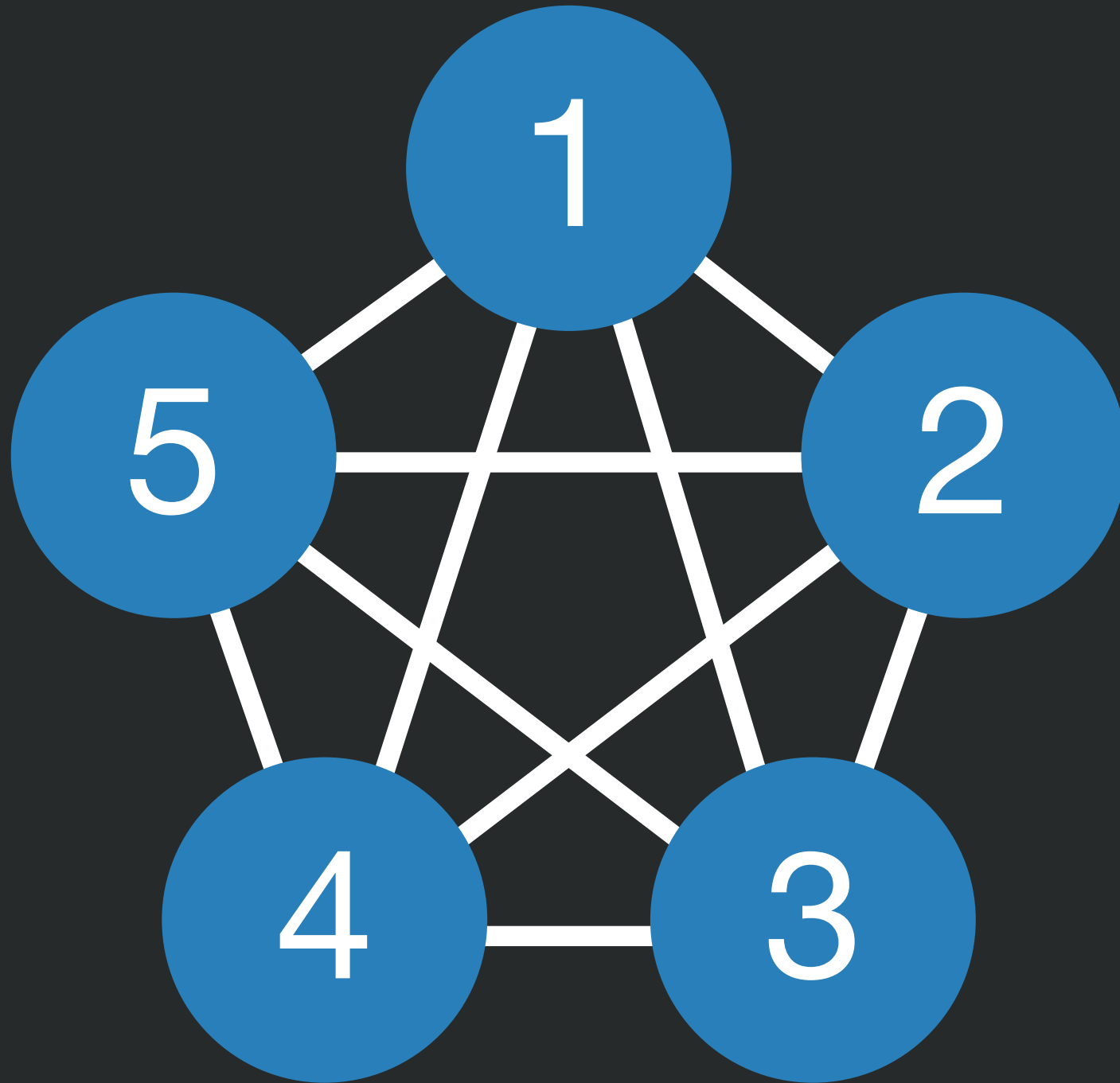


**Why do systems become so complicated?**

# Understand complexity with Metcalfe's Law

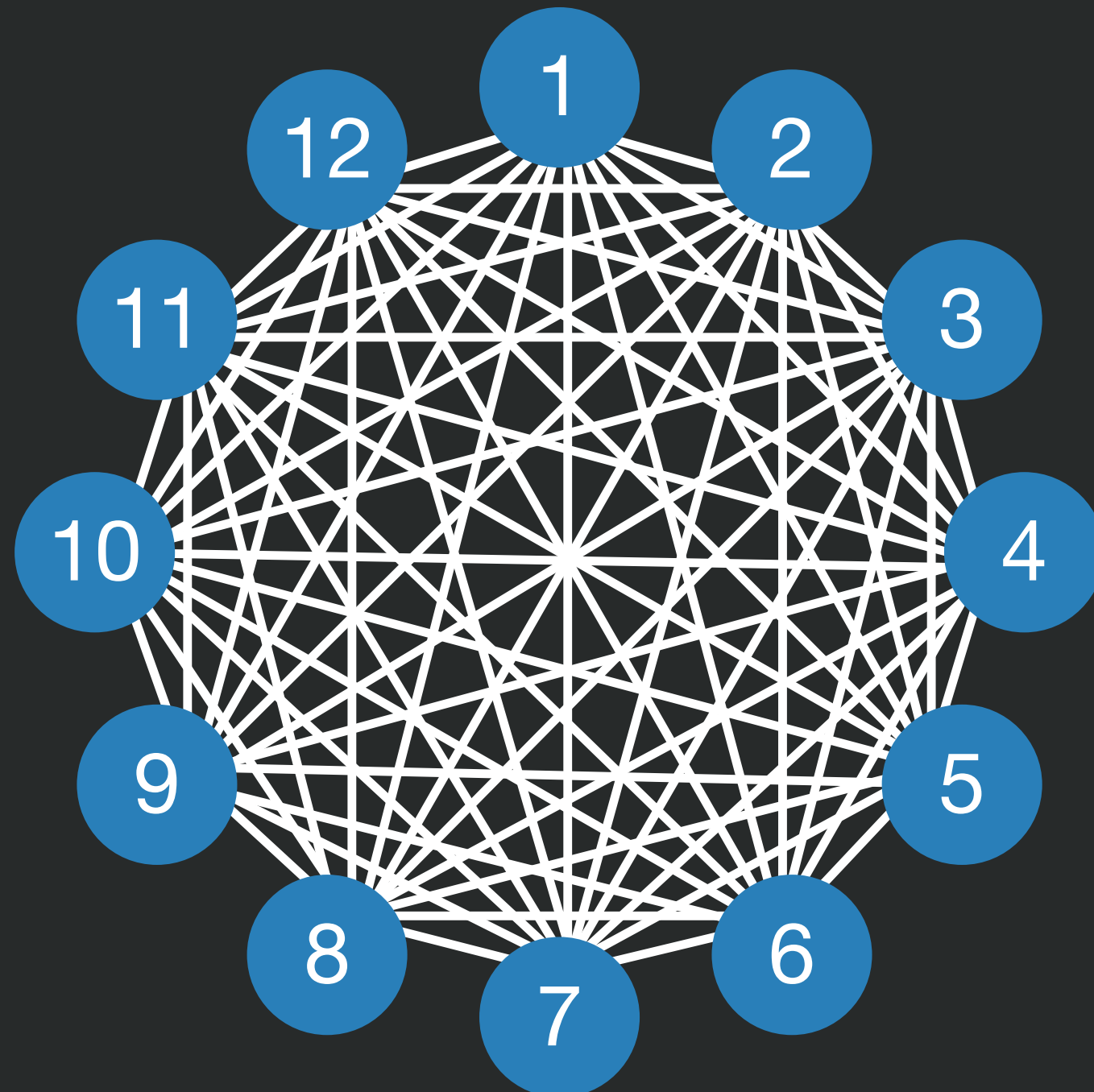
$$\frac{n(n-1)}{2}$$





10

$$\frac{n(n-1)}{2}$$



**66**

**Complexity is caused by:  
quadratic increase in  
connections**

**How do we reduce complexity?**

**Design reduces dependencies**



**Org structure  
or  
Code structure?**

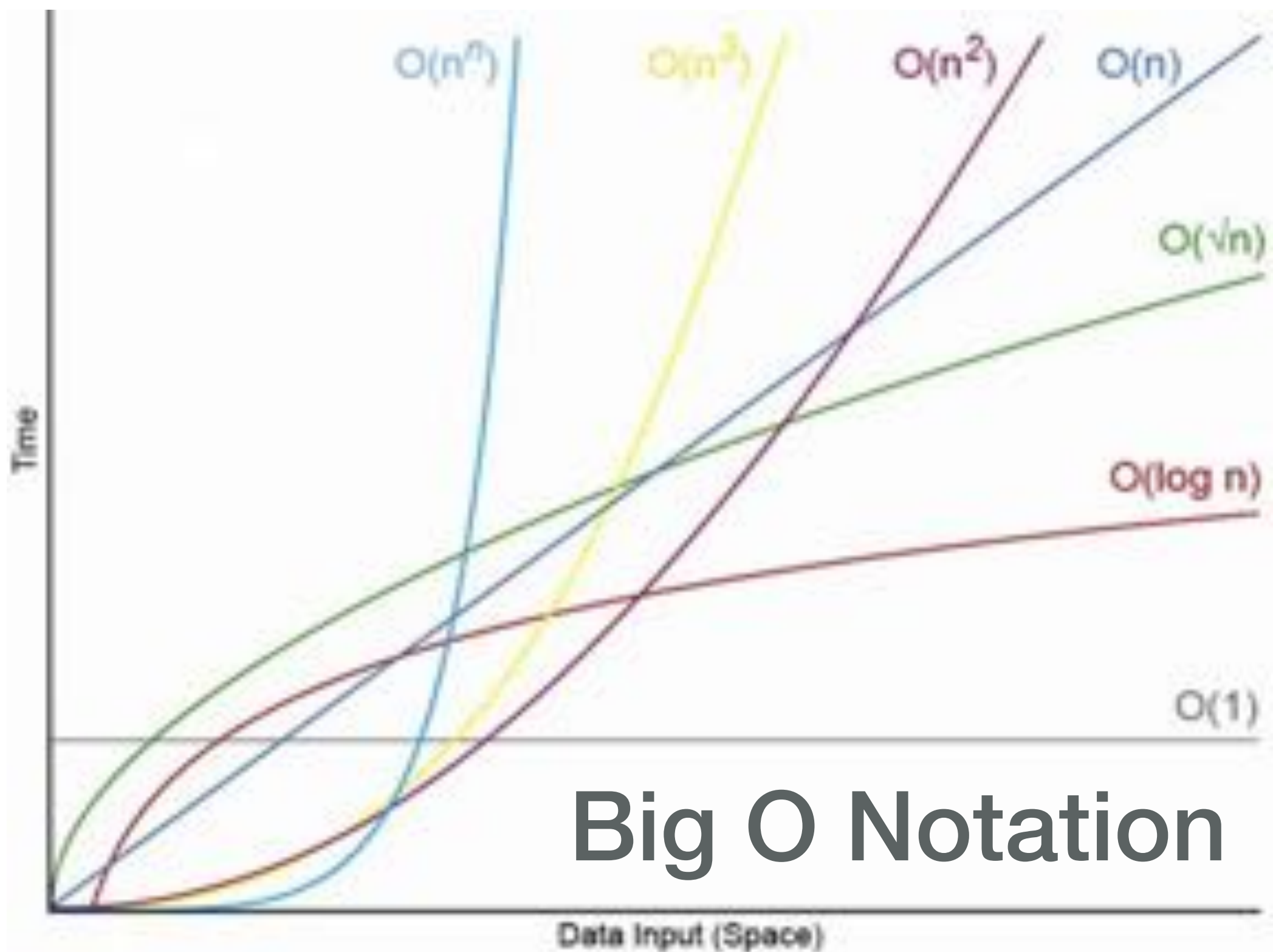


# Summary:

Reduce connections to increase simplicity.

Remember Metcalfe's Law!

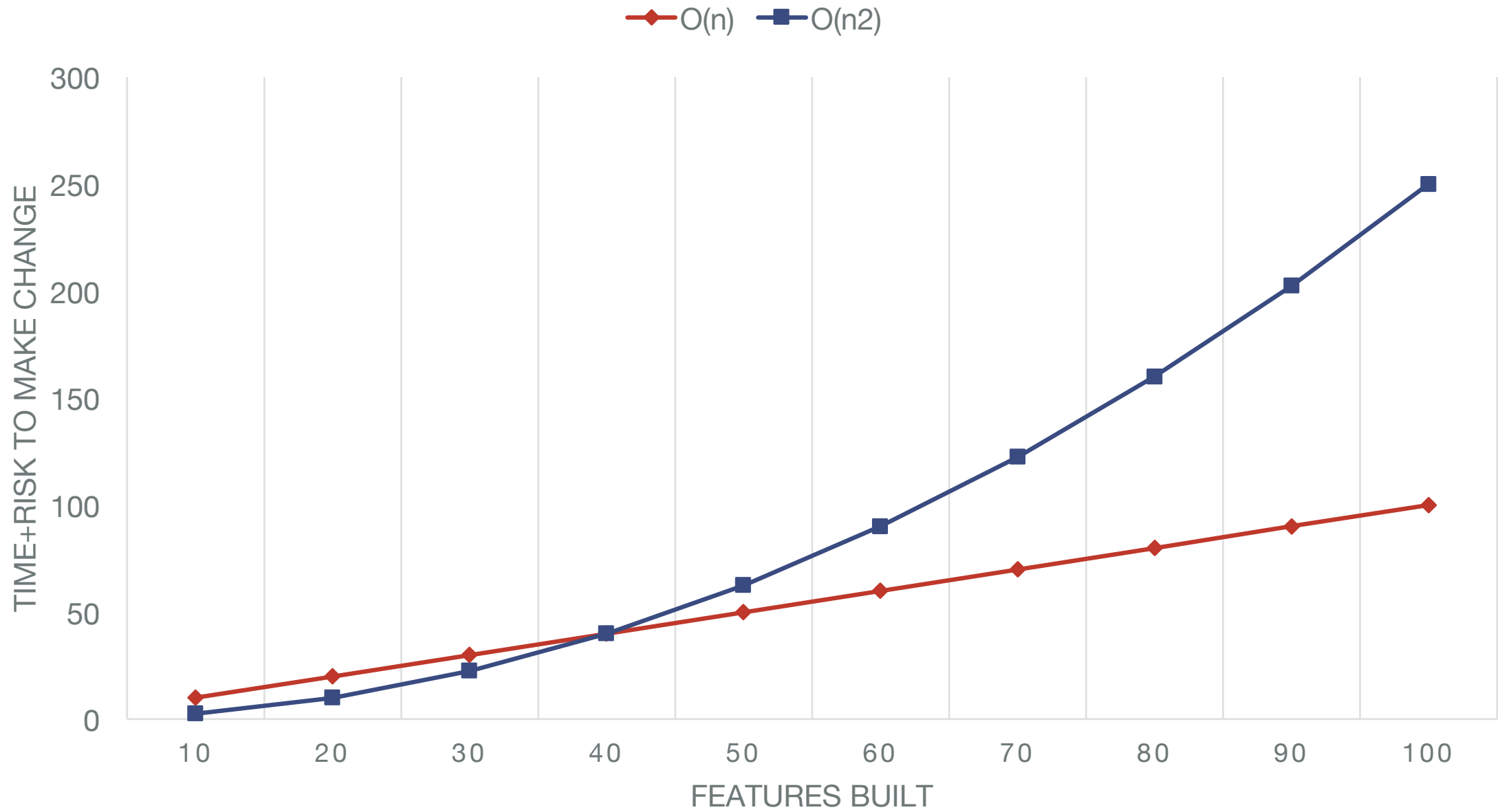
But what about complexity  
over *TIME*?



Go slow to go fast with  
the right work algorithm

*Big O*

# CODE CHANGE COMPLEXITY



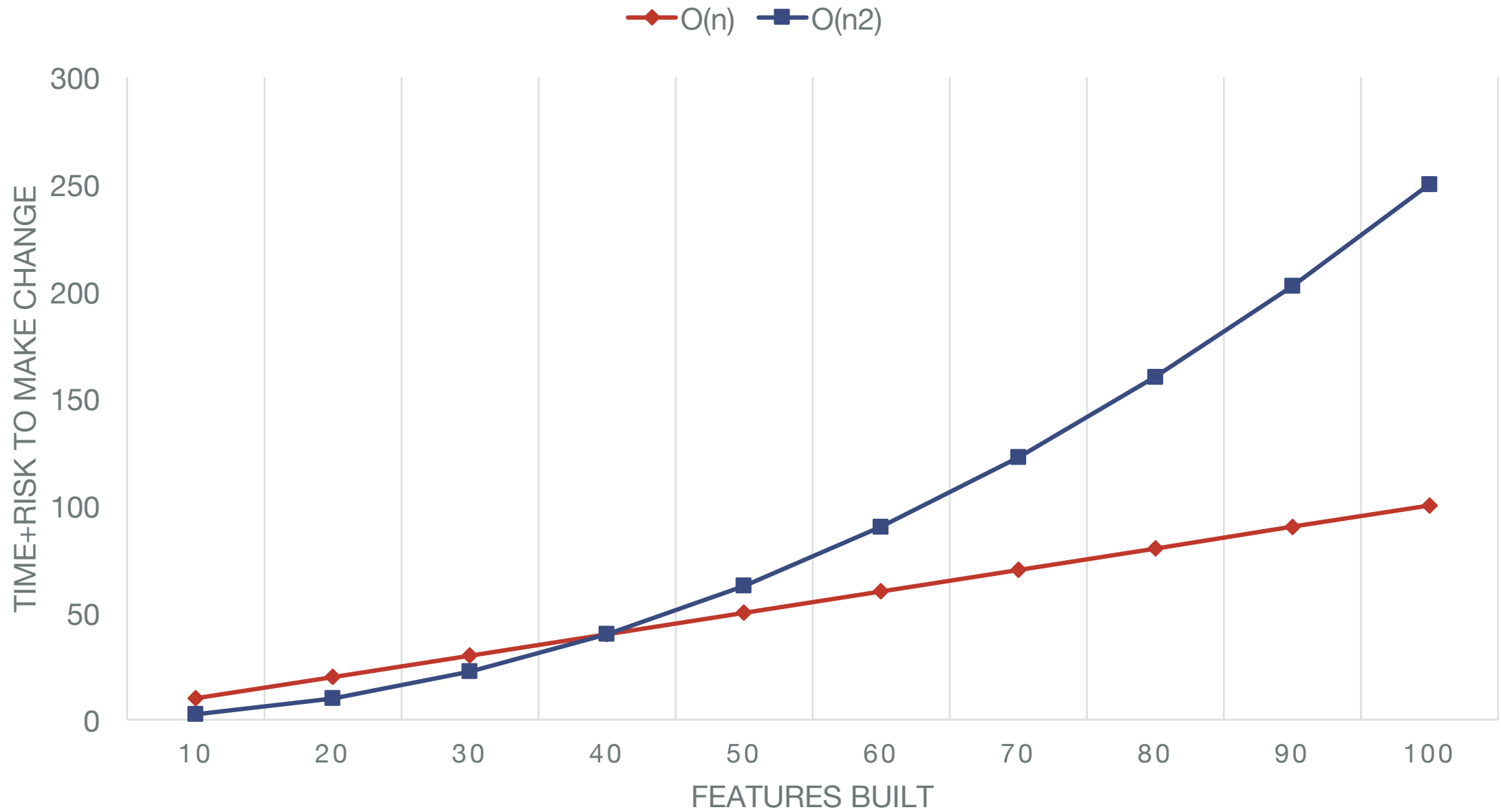
# Clean Code gives $O(n)$

- Easy to read
- SOLID design
- Boy scout refactoring
- Self-testing
- TDD

# Messy code gives $O(n^2)$

- Manual regression testing
- Spaghetti dependencies
- Hard to understand

# CODE CHANGE COMPLEXITY





**Your algorithm of work  
determines order of time  
complexity**

# In summary

Clean code decreases dev cost over time. Go slow to go fast.

Think about work your algorithm with Big O!

**We're so busy! Why don't we  
get stuff done?**

A high-angle, wide shot of a multi-lane road completely filled with cars, buses, and motorcycles, illustrating a severe traffic jam. The vehicles are packed closely together, stretching far into the distance. The scene is set in a city with trees lining the right side of the road.

**We're so busy! Why don't we  
get stuff done?**

Credit: <http://www.autoevolution.com/>

SHOCKWAVE TRAFFIC JAMS  
RECREATED FOR FIRST TIME

Footage courtesy of  
University of Nagoya,  
Nagoya, Japan

[youtu.be/Suugn-p5C1M](https://youtu.be/Suugn-p5C1M)



# Maximise efficiency with Queueing Theory

Little's Law

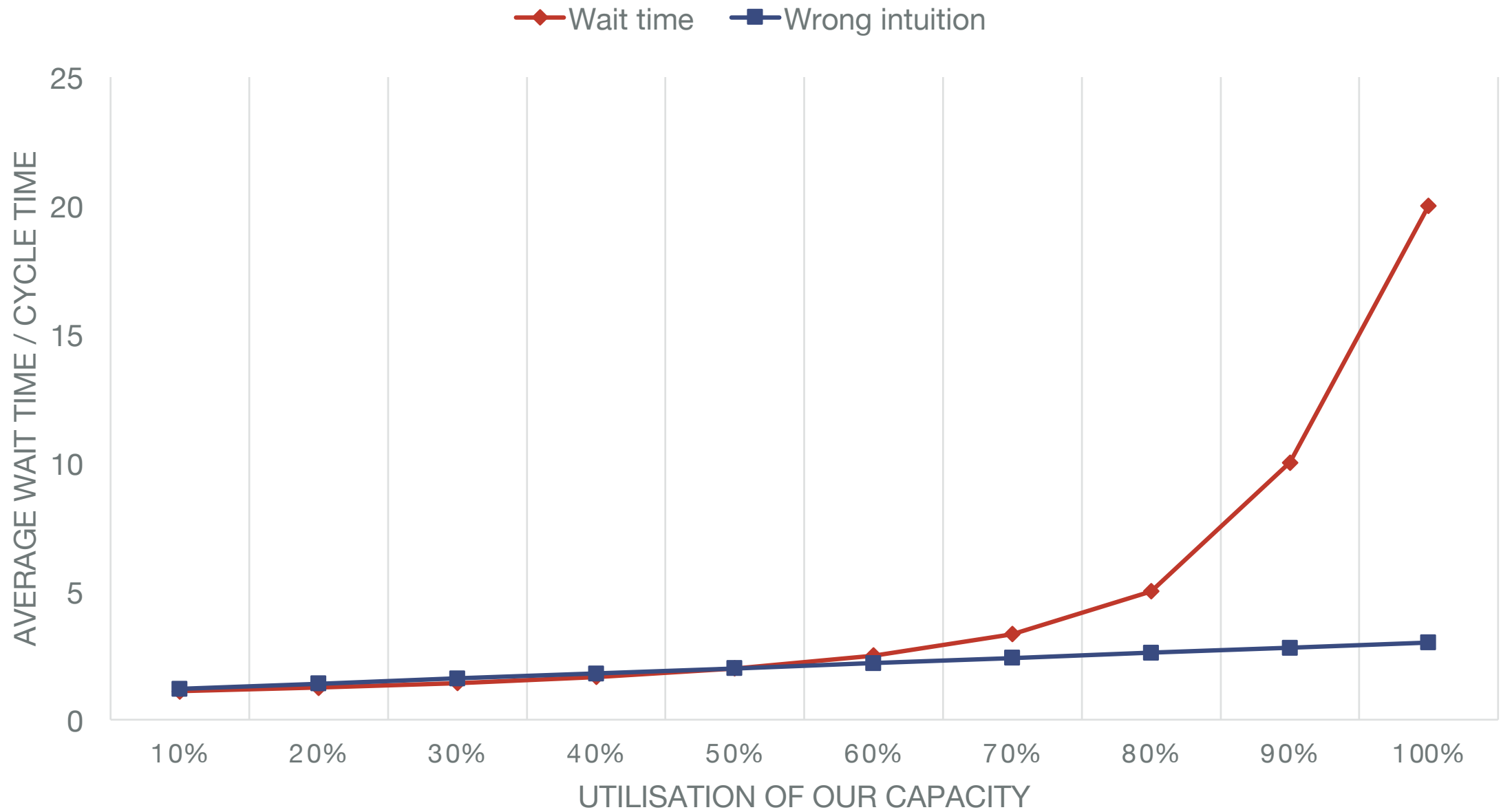
and

Kingman's Formula

# Kingman's Formula

$$\textit{Average Wait Time} \propto \left( \frac{\textit{Utilisation}}{1 - \textit{Utilisation}} \right)$$

# HIGH UTILISATION SHOOTS UP WAIT TIME





# Over-utilisation causes jams

$$\textit{Average Wait Time} \propto \left( \frac{\textit{Utilisation}}{\mathbf{1} - \textit{Utilisation}} \right)$$

**Utilisation is hard to manage**

# Little's law

$$\textit{Avg Wait} \approx \frac{\textit{Avg Work in Progress}}{\textit{Avg Throughput}}$$

Reduce *Work in Progress*

to

reduce *Utilisation*

to

reduce *Wait Time*

*“Queues are the root cause of the majority of economic waste in product development.”*

**Donald G. Reinertsen**

A photograph of a waterfall with water cascading down rocks, creating a sense of flow and movement. The water is a deep blue color, and the rocks are dark and jagged.

The  
Principles of  
Product  
Development

# ***FLOW***

*Second Generation  
Lean Product Development*

DONALD G. REINERTSEN

# In summary

Avoid congestion and increase flow

- by reducing work in progress and
- reducing utilisation

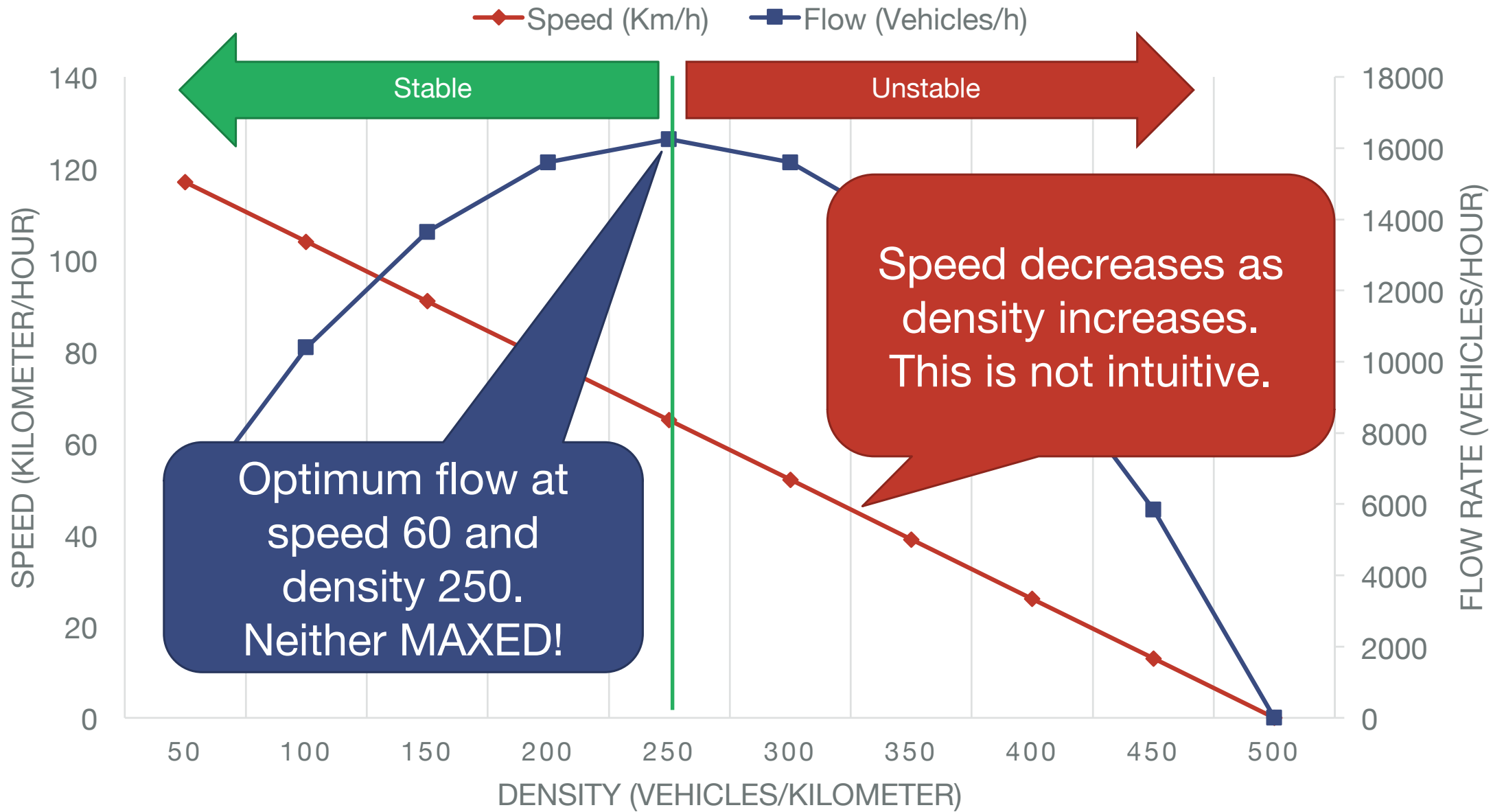
ECONOMICALLY  
OPTIMAL  
UTILIZATION





$$\frac{\textit{Vehicles}}{\textit{Hour}} = \frac{\textit{Meters}}{\textit{Hour}} \cdot \frac{\textit{Vehicles}}{\textit{Meter}}$$

# OPTIMAL FLOW



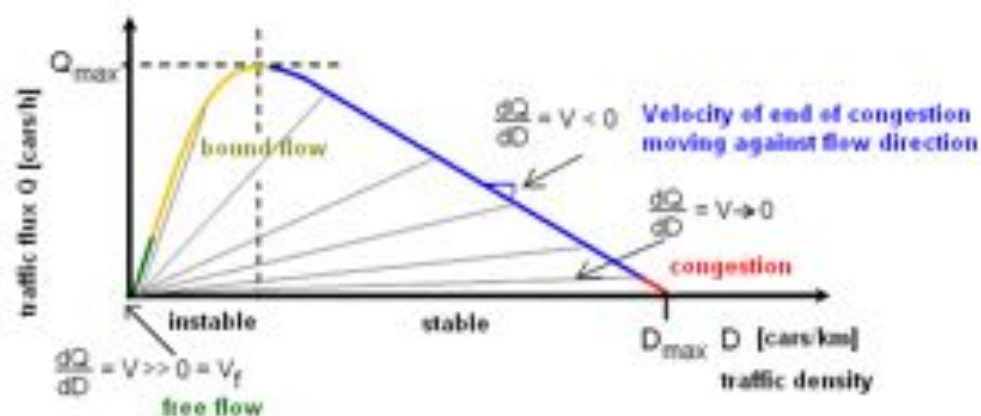
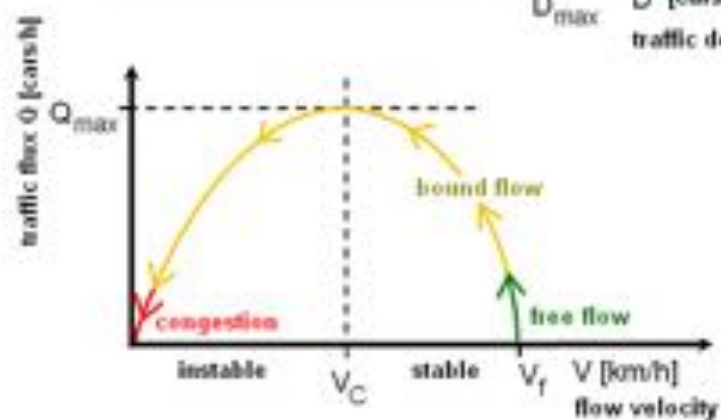
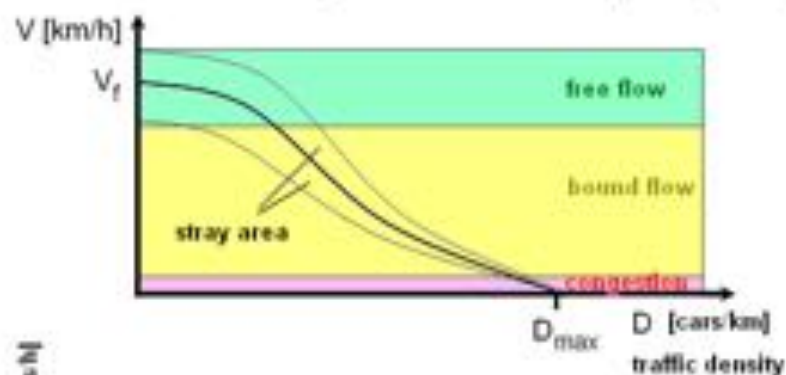
$$\textit{Speed} = (1 - \textit{Density} \cdot \textit{JamDens}) \cdot \textit{MaxSpeed}$$

## Fundamental diagram of traffic flow

Fundamental equation of traffic flow:

$$Q = D \cdot V$$

Source: Hendrik Ammer, Fakultät Verkehrswissenschaften, Dresden, Germany



$V_f$  = "free velocity" - maximum velocity on free lane, selectable by the driver depending on car, skill etc.

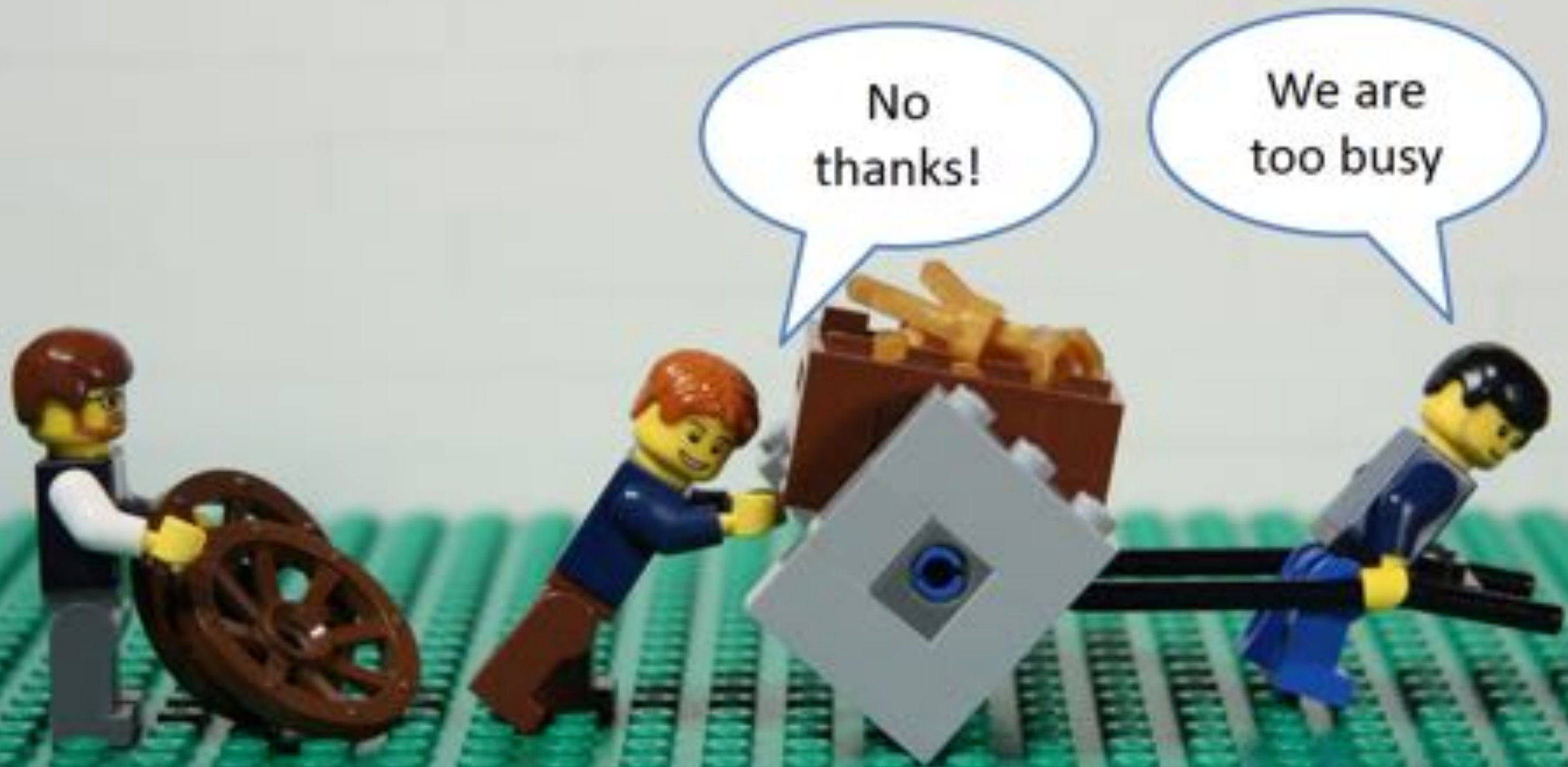
$V_C$  = "critical velocity" with maximum traffic flux (about 70 ... 100 km/h)

# How does this apply to software?

- $Flow = Speed \cdot Density$
- $Velocity = Throughput = Flow$  (avg # features delivered per week)
- $WIP = Density$  (avg # features started but not completed)
- $Cycle\ time = \frac{1}{Speed}$  (avg time it takes to complete a feature)
- $Throughput = \frac{WIP}{Cycle\ Time}$  (aka Little's Law)

$$Velocity = \frac{Avg\ features\ in\ progress}{Avg\ time\ to\ complete\ a\ feature}$$

# Are you too busy to improve?



Improve continuously with

$$A = Pe^{rt}$$

# Continuous compound interest

**Amount**

© mathwarehouse.com

↓

$$A = Pe^{rt}$$

rate of interest  
time in years



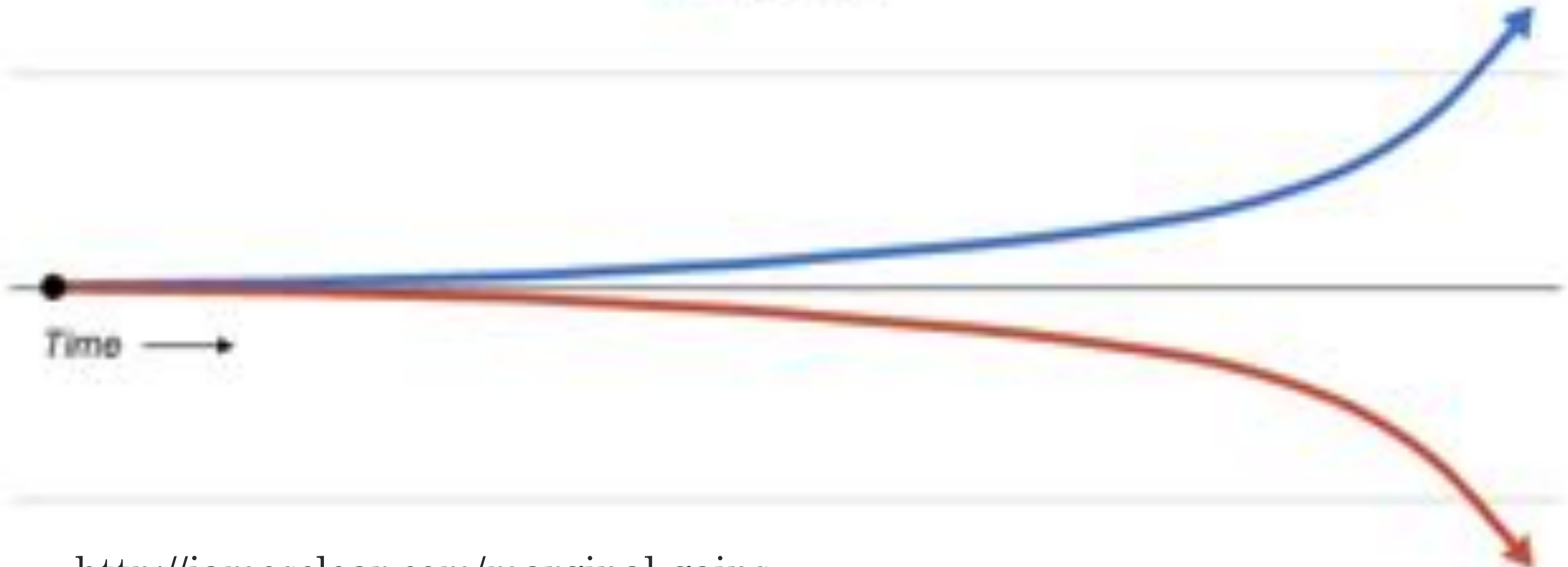
**Principal**

the mathematical constant **e**



# Aggregation of Marginal Gains

- 1% Improvement
- 1% Decline



<http://jamesclear.com/marginal-gains>

# *Improvement = $e^{rt}$*

- $r = 1\%$  per week (improvement rate)
- $t = 104$  weeks/2 years (time in weeks)

This gives us

- 294% improvement over 2 years!

$$e^{rt}$$

- $r = -1\%$  per week (decay rate)
- $t = 104$  weeks/2 years (time in weeks)

This gives us

- 34% of original
- Degraded 66% over 2 years!

*Is this how technical debt behaves?*

# In summary

Improve 1% every week.

Improvements compound.



Simplify by reducing dependencies



You need quality to keep going fast



Do less at once to go fast



Continuous improvement compounds

# Other equations

- Entropy
- Bayesian Inference
- The software engineering equation
- Yours?



DISCUSS.

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